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Model and Rule Transformation

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Abstract: In the framework of graph transformation, simulation rules are well-known to define the operational behavior of visual models. Moreover, it has been shown already how to construct animation rules in a domain specific layout from simulation rules. An important requirement of this construction is the semantical correctness which has not yet been considered. In this paper we give a precise definition for *simulation-to-animation* (*S2A*) model and rule transformations. Our main results show under which conditions semantical correctness can be obtained. The results are applied to analyze the *S2A* transformation of a Radio Clock model.

Keywords: graph transformation, model and rule transformation, semantical correctness, simulation, animation

1 Introduction

In recent years, visual models represented by graphs have become very popular in model-based software development, as the wide-spread use of UML and Petri nets proves. For the definition of an operational semantics for visual models, the transformation of graphs plays a similar central role as term rewriting in the traditional case of textual models. The area of graph transformation provides a rule-based setting to express the semantics of visual models (see e.g. [Roz97]). The objective of *simulation rules* is their application to the states of a visual model, deriving subsequent model states, thus characterizing system evolution. A *simulation scenario*, i.e. a sequence of such simulation steps can be visualized by showing the states before and after each simulation rule application as graphs.

For validation purposes, simulation may be extended to a domain specific view, called *animation view* [EB04, EE05b, EHKZ05], which allows to define scenario visualizations in the layout of the application domain. The animation view is defined by extending the alphabet of the original visual modeling language by symbols representing entities from the application domain. The simulation rules for a specific visual model are translated to the animation view by performing a *simulation-to-animation model and rule transformation* (*S2A* transformation), realizing a consistent mapping from simulation steps to animation steps which can be visualized in the animation view layout. *S2A* transformation is defined by a set of *S2A* graph transformation rules, and an additional formal construction allowing to apply *S2A* rules to simulation rules, resulting in a new set of graph transformation rules, called *animation rules*.

Comparable theoretical research in the area of applying graph transformation rules to rules has been done by Parisi-Presicce [PP96]. His approach has provided the basis of our definition of *S2A* transformations which additionally allows to transform not only the rule interfaces, and which also treats negative application conditions (NACs), both for the transforming rules and for the transformed rules.

An important requirement is the *semantical correctness* of the *S2A* transformation in the sense that the behavior of the original model is preserved in the animation view. In this paper, we give a formal definition for *S2A* transformations and show under which conditions semantical correctness can be obtained. In our approach, an *S2A* transformation generates one animation rule for each simulation rule. Hence, our notion of semantical correctness implies that each animation step (obtained by applying an animation rule) corresponds to a simulation step of the original model. Please note that there are more general definitions for the semantical correctness of model transformations which establish a correspondence between one simulation step in the source model and a sequence of simulation steps in the target model. For *S2A* transformation it is sufficient to relate single simulation and animation steps. Intermediate animation states providing smooth state transitions are possible nonetheless: They are defined by enriching an animation rule by animation operations to specify continuous changes of object properties. Since animation operations leave the states before and after a rule application unchanged, they do not influence the semantical correctness of *S2A* transformation. Our approach has been implemented in the generic visual modeling environment GENGED [Gen]. The implementation includes an animation editor to define animation operations visually, and to export animation scenarios to the SVG format [WWW03].

There exist related tool-oriented approaches, where different visual representations are used to visualize a model's behavior. One example is the *reactive animation* approach by Harel [HEC03], where behavior is specified by UML diagrams. The animated representation of the system behavior is implemented by linking UML tools to pure animation tools like Macromedia FLASH or DIRECTOR [Mac04]. Hence, the mapping from simulation to animation views happens at the implementation level and is not specified formally. Analogously, different Petri net tools also offer support for customized Petri net animations (e.g. the SimPEP tool [Gra99] to animate transition firings of low-level Petri nets). In general, approaches to enhance the front end of CASE tools for simulating/animating the behavior of models are restricted to one specific modeling language. In our approach we integrate animation views at model level with graph transformation representations for different visual modeling languages based on a formal specification. This provides the model designer with more flexibility, as the modeling language to be enhanced by animation features, can be freely chosen.

The paper is organized as follows: Section 2 presents the basic concepts of simulation and animation, illustrated by our case study in Section 3. In Section 4, the main result on semantical correctness of *S2A* transformation is given in the case without NACs. Extensions to cope with NACs are discussed. Explicit proofs for the case with NACs, and the semantical correctness of the complete case study is presented in the technical report [EEE06]. Section 5 discusses related work, and Section 6 concludes the paper.

2 Basic Concepts of Simulation and Animation

We use typed algebraic graph transformation systems (TGTS) in the double-pushout-approach (DPO) [EEPT06] which have proven to be an adequate formalism for visual language (VL) modeling. A VL is modeled by a type graph capturing the definition of the underlying visual alphabet, i.e. the symbols and relations which are available. Sentences or diagrams of the VL are given by graphs typed over the type graph. We distinguish abstract and concrete syntax in alphabets and models, where the concrete syntax includes the abstract symbols and relations, and additionally defines their layout. Formally, a VL can be considered as a subclass of graphs typed over a type graph TG in the category \mathbf{Graphs}_{TG} .

For behavioral diagrams like Statecharts, an operational semantics can be given by a set of simulation rules P_S , using the abstract syntax of the modeling VL. A simulation rule $p = (L \leftarrow I \rightarrow R) \in P_S$ is a graph transformation rule, consisting of a left-hand side L , an interface I , a right-hand side R , and two injective morphisms. Applying rule p to a graph G means to find a match of $L \xrightarrow{m} G$ and to replace the occurrence $m(L)$ of L in G by R leading to the target graph G' . In the DPO approach, the deletion of $m(L)$ and the addition of R are described by two pushouts (a DPO) in the category \mathbf{Graphs}_{TG} of typed graphs. A rule p may be extended by a set of *negative application conditions* (NACs) [EEPT06], describing situations in which the rule should not be applied to G . Formally, match $L \xrightarrow{m} G$ satisfies NAC $L \xrightarrow{n} N$ if there does not exist an injective graph morphism $N \xrightarrow{x} G$ with $x \circ n = m$. A sequence $G_0 \Rightarrow G_1 \Rightarrow \dots \Rightarrow G_n$ of graph transformation steps is called *transformation* and denoted as $G_0 \xRightarrow{*} G_n$. A transformation $G_0 \xRightarrow{*} G_n$, where rules from P are applied as long as possible (i.e. as long as matches can be found satisfying the NACs), is denoted by $G_0 \xRightarrow{P!} G_n$.

We define a model's *simulation language* VL_S , typed over the simulation alphabet TG_S , as a sublanguage of the modeling language VL , such that all diagrams $G_S \in VL_S$ represent different states during simulation. Based on VL_S , the operational semantics of a model is given by a *simulation specification*.

Definition 1 (Simulation Specification) Given a visual language VL_S typed over TG_S , i.e. $VL_S \subseteq \mathbf{Graphs}_{TG_S}$, a *simulation specification* $SimSpec_{VL_S} = (VL_S, P_S)$ over VL_S is given by a TGTS (TG_S, P_S) s.t. VL_S is closed under simulation steps, i.e. $G_S \in VL_S$ and $G_S \Rightarrow H_S$ via $p_S \in P_S$ implies $H_S \in VL_S$. The rules $p_S \in P_S$ are called simulation rules.

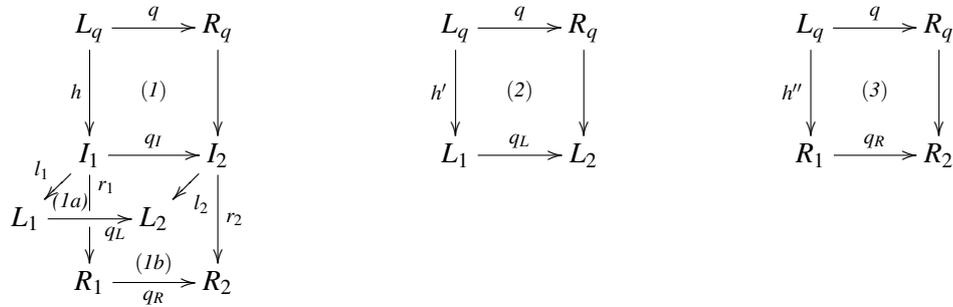
In order to transform a simulation specification to an animation view, we define an *S2A transformation* $S2A = (S2AM, S2AR)$ consisting of a simulation-to-animation model transformation $S2AM$, and a corresponding rule transformation $S2AR$. The $S2AM$ transformation applies $S2A$ transformation rules from a rule set Q to each $G_S \in VL_S$ as long as possible, adding symbols from the application domain to the model state graphs. The resulting set of graphs comprises the animation language VL_A .

Definition 2 (*S2AM-Transformation*) Given a simulation specification $SimSpec_{VL_S} = (VL_S, P_S)$ with VL_S typed over TG_S and a type graph TG_A , called animation type graph, with $TG_S \subseteq TG_A$, a *simulation-to-animation model transformation*, short *S2AM-transformation*, $S2AM : VL_S \rightarrow VL_A$ is given by $S2AM = (VL_S, TG_A, Q)$ where (TG_A, Q) is a TGTS with non-deleting rules $q \in Q$,

and S2AM-transformations $G_S \xrightarrow{Q} G_A$ with $G_S \in VL_S$. The *animation language* VL_A is defined by $VL_A = \{G_A \mid \exists G_S \in VL_S \ \& \ G_S \xrightarrow{Q} G_A\}$. This means $G_S \xrightarrow{Q} G_A$ implies $G_S \in VL_S$ and $G_A \in VL_A$, where each intermediate step $G_i \xrightarrow{q_i} G_{i+1}$ is called *S2AM-step*.

Our aim is not only to transform model states but to obtain a complete animation specification, including animation rules, from the simulation specification. Hence, we define a construction allowing us to apply the S2A transformation rules from Q also to the simulation rules. The following definition extends the construction for rewriting rules by rules given by Parisi-Presicce in [PP96], where a rule q is only applicable to a rule p if it is applicable to the interface graph of p . In this paper, we want to add animation symbols to simulation rules even if the S2A transformation rule is *not* applicable to the interface of the simulation rule. Hence, we distinguish three cases in Def. 3. Case (1) corresponds to the notion of rule rewriting in [PP96], adapted to non-deleting S2A transformation rules. In Case (2), the S2A transformation rule q is not applicable to the interface, but only to the left-hand side of a rule p , and in Case (3), q is only applicable to the right-hand side of p .

Definition 3 (Transformation of Rules by Non-Deleting Rules) Given a non-deleting rule $q = (L_q \rightarrow R_q)$ and a rule $p_1 = (L_1 \xleftarrow{l_1} I_1 \xrightarrow{r_1} R_1)$, then q is applicable to p_1 leading to a *rule transformation step* $p_1 \xrightarrow{q} p_2$, if the precondition of one of the following three cases is satisfied, and $p_2 = (L_2 \xleftarrow{l_2} I_2 \xrightarrow{r_2} R_2)$ is defined according to the corresponding construction.



Case (1)

Precondition (1): There is a match $L_q \xrightarrow{h} I_1$.

Construction (1): I_2 , L_2 , and R_2 are defined by pushouts (1), (1a) and (1b), leading to injective morphisms l_2 and r_2 .

Case (2)

Precondition (2): There is no match $L_q \xrightarrow{h} I_1$, but a match $L_q \xrightarrow{h'} L_1$.

Construction (2): L_2 is defined by pushout (2), and $I_2 = I_1$, $R_2 = R_1$, $r_2 = r_1$, and $l_2 = q_L \circ l_1$.

Case (3)

Precondition (3): There are no matches $L_q \xrightarrow{h} I_1$ and $L_q \xrightarrow{h'} L_1$, but there is a match $L_q \xrightarrow{h''} R_1$.

Construction (3): R_2 is defined by pushout (3), and $L_2 = L_1$, $I_2 = I_1$, $l_2 = l_1$, and $r_2 = q_L \circ r_1$.

The transformation of rules defined above allows now to define an *S2AR* transformation of rules, leading to an *S2A* transformation $S2A = (S2AM, S2AR)$ from the simulation specification $SimSpec_{VL_S}$ to the animation specification $AnimSpec_{VL_A}$.

Definition 4 (*S2AR-Transformation*) Given a simulation specification $SimSpec_{VL_S} = (VL_S, P_S)$ and an *S2AM*-transformation $S2AM = (VL_S, TG_A, Q)$ then a *simulation-to-animation rule transformation*, short *S2AR-trafo*, $S2AR : P_S \rightarrow P_A$ is given by $S2AR = (P_S, TG_A, Q)$ and *S2AR transformation sequence* $p_S \xrightarrow{Q} p_A$ with $p_S \in P_S$, where rule transformation steps $p_1 \xrightarrow{q} p_2$ with $q \in Q$ (see Def. 3) are applied as long as possible.

The *animation rules* P_A are defined by $P_A = \{p_A \mid \exists p_S \in P_S \wedge p_S \xrightarrow{Q} p_A\}$.

This means $p_S \xrightarrow{Q} p_A$ implies $p_S \in P_S$ and $p_A \in P_A$, where each intermediate step $p_i \xrightarrow{q_i} p_{i+1}$ is called *S2AR-step*.

Definition 5 (*Animation Specification and S2A Transformation*) Given a simulation specification $SimSpec_{VL_S} = (VL_S, P_S)$, an *S2AM* transformation $S2AM : VL_S \rightarrow VL_A$ and an *S2AR* transformation $S2AR : P_S \rightarrow P_A$, then

1. $AnimSpec_{VL_A} = (VL_A, P_A)$ is called *animation specification*, and each transformation step $G_A \xrightarrow{p_A} H_A$ with $G_A, H_A \in VL_A$ and $p_A \in P_A$ is called *animation step*.
2. $S2A : SimSpec_{VL_S} \rightarrow AnimSpec_{VL_A}$, defined by $S2A = (S2AM, S2AR)$ is called *simulation-to-animation model and rule transformation*, short *S2A transformation*.

3 Case Study: Radio Clock

In this section, we illustrate the main concepts of Section 2 by the well-known Radio Clock case study from Harel [Har87]. The behavior of a radio clock is modeled by the nested Statechart shown in Fig. 1 (a). The radio clock display can show alternatively the time, the date or allows to set the alarm time. The changes between the modes are modeled by transitions labeled with the event *Mode*. The nested state *Alarm* allows to change to modes for setting the hours and the minutes (transition *Select*) of the alarm time. A *Set* event increments the number of hours or minutes which are currently displayed.

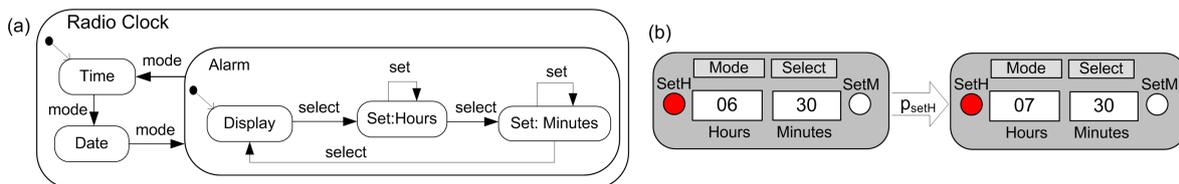


Figure 1: Radio Clock Statechart (a), and Animation View Snapshots (b)

A domain-specific animation view of the Radio Clock is illustrated in Fig. 1 (b). The two snapshots from a possible simulation run of the Statechart in Fig. 1 (a) correspond to the active

state Set:Hours before and after the set event has been processed. The animation view shows directly the current display of the clock and indicates by a red light that in the current state the hours may be set. Furthermore, buttons are shown either to proceed to the state where the minutes may be set (button Select), or to switch back to the Time display (button Mode).

The abstract syntax graph of the Radio Clock Statechart is the given by the graph G_I in Fig. 2.

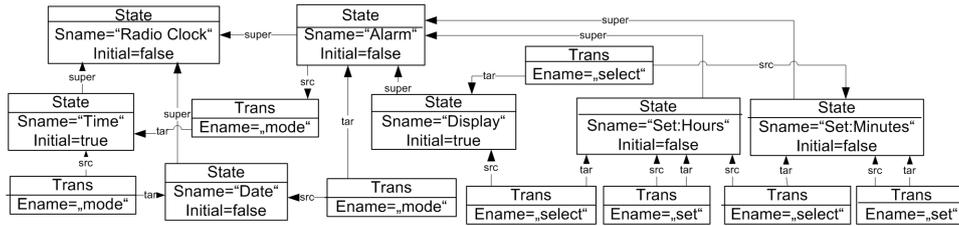


Figure 2: Abstract Syntax Graph G_I of the Radio Clock Statechart

The set of model-specific simulation rules $P_S = \{p_{addObject}, p_{addEvent}, p_{downTime}, p_{downDisp}, p_{upAlarm}, p_{upClock}, p_{modeTD}, p_{modeDA}, p_{modeAD}, p_{selectH}, p_{selectM}, p_{selectD}, p_{setH}, p_{setM}\}$ to be applied to G_I contains initialization rules which generate the object node with attribute values for the initial alarm time, set the current pointer to the top level state Radio Clock, and fill the event queue. Additional simulation rules are defined which realize the actual simulation, processing the events in the queue. For each superstate there is a rule moving the current pointer from the superstate down to its initial substate. Analogously, there are rules moving the pointer from a substate to its superstate. For each transition there is a rule which moves the pointer from the source state of the transition to its target state and removes the triggering event from the queue. The full set P_S of simulation rules is given in [EEE06]. Fig. 3 shows the sample simulation rule p_{setH} for the transition set whose source and target is the state Set:Hours. In addition to processing the event set, this rule increments the hour value of the current alarm time.

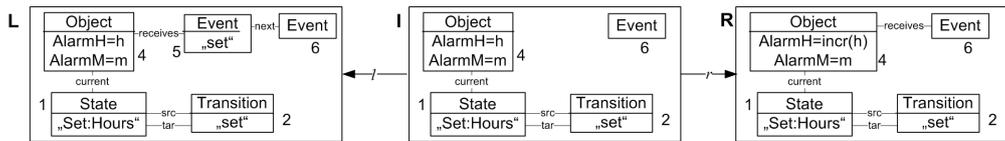


Figure 3: A Simulation Rule p_{setH}

The simulation specification $SimSpec_{VL_S} = (VL_S, P_S)$ for the Radio Clock consists of the simulation language VL_S typed over TG_S , where TG_S is the simulation alphabet depicted in the left-hand side of Fig. 4, P_S is the set of simulation rules, and VL_S consists of all graphs that can occur in any Radio Clock simulation scenario: $VL_S = \{G_S | \exists G_I \xrightarrow{P_S^*} G_S\}$, where G_I is the initial graph shown in Fig. 2.

Fig. 4 shows the animation view type graph TG_A , which is a disjoint union of the simulation alphabet TG_S , and the new visualization alphabet TG_V shown in the right part of Fig. 4, which models the visualization symbols for a domain-specific view of the radio clock behavior. The three modes of the clock are visualized by five different displays: a date display, a time display,

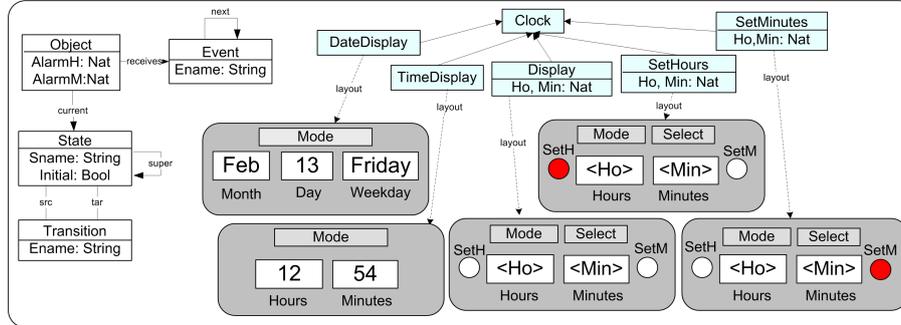


Figure 4: Simulation and Animation Alphabet

and three alarm displays showing the alarm time but differing in the states of two red lights which indicate the states Display (both lights off), Set:Hours (light SetH on), and Set:Minutes (light SetM on).

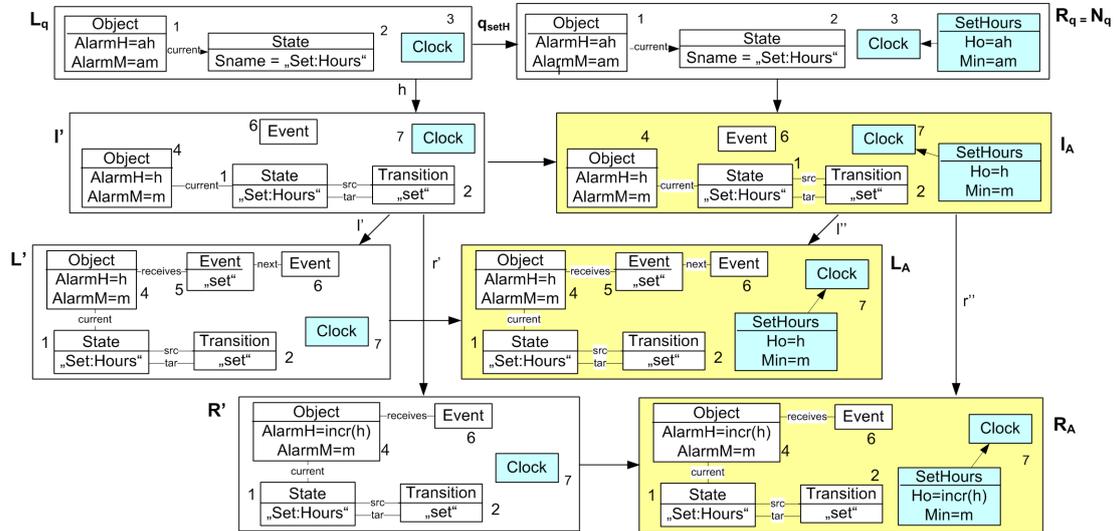
The $S2A$ transformation rules $Q = \{q_{Clock}, q_{Date}, q_{Time}, q_{Disp}, q_{SetH}, q_{SetM}\}$ add visualization symbols to the simulation rule graphs and to the initial radio clock graph. The initial $S2A$ rule q_{Clock} adds the root symbol Clock to all graphs it is applied to. The remaining $S2A$ rules add visualization symbols depending on the state of the current pointer. We visualize only basic states which do not have any substates. Superstates are not shown in the animation view, as they are considered as transient, abstract states which are active on the way of the current pointer up and down the state hierarchy between two basic states, but have no concrete layout themselves.

The full set Q of $S2A$ rules is given in [EEE06]. The top row of Fig. 5 shows the sample $S2A$ transformation rule q_{setH} which adds a SetHours symbol and links it to the clock symbol in the case that the current pointer points to the state named “Set:Hours”. The attributes are set accordingly. Note that each $S2A$ rule q has to be applied at most once at the same match, which is formalized by a NAC $L_q \rightarrow N_q$, such that N_q and R_q are isomorphic. The Radio Clock $S2AM$ transformation $S2AM : VL_S \rightarrow VL_A$ is given by $S2AM = (VL_S, TG_A, Q)$ with animation language $VL_A = \{G_A | \exists G_S \in VL_S : G_S \xrightarrow{Q} G_A\}$. The Radio Clock $S2AR$ transformation $S2AR : P_S \rightarrow P_A$ is given by $S2AR = (P_S, TG_A, Q)$ with animation rules $P_A = \{p_A | \exists p_S \in P_S : p_S \xrightarrow{Q} p_A\}$.

A sample $S2AR$ transformation step $p'_{setH} \xrightarrow{q_{setH}} p^A_{setH}$ is shown in Fig. 5. Here, $S2A$ rule $L_q \xrightarrow{q_{setH}} R_q$ is applied to the rule p'_{setH} , according to Case (1) of Def. 3. Rule $p'_{setH} = (L' \leftarrow I' \rightarrow R')$ in Fig. 5 corresponds to rule $p_1 = (L_1 \leftarrow I_1 \rightarrow R_1)$ in Def. 3. The result of the rule rewriting step in Fig. 5 is rule $p^A_{setH} = (L_A \leftarrow I_A \rightarrow R_A)$, which corresponds to rule $p_2 = (L_2 \leftarrow I_2 \rightarrow R_2)$ in Def. 3. Note that variables for node attributes can be assigned to other variables or to expressions. For instance, in Fig. 5, the variable h for attribute AlarmH in I' is assigned to the expression $incr(h)$ in R' by the morphism $I' \xrightarrow{r'} R'$. Hence, a resulting animation rule can contain variables or expressions for attributes to be assigned to corresponding attribute values in graphs when the animation rule is applied.

p^A_{setH} is a completely transformed animation rule, since no more $S2A$ rules are applicable to it.

The Radio Clock animation specification $AnimSpec_{VL_A} = (VL_A, P_A)$ based on the $S2A$ trans-


 Figure 5: S2A Transformation Step $p'_{setH} \xrightarrow{q_{setH}} p^A_{setH}$

formation $S2A = (S2AM, S2AR)$ is given by the animation language VL_A , obtained by the Radio Clock $S2AM$ transformation, and the animation rules P_A , obtained by the Radio Clock $S2AR$ transformation. The full set P_A of animation rules is given in [EEE06].

Fig. 6 shows a sample animation scenario in the concrete notation of the animation view, where animation rules from P_A are applied. The first state of the scenario in Fig. 6 is obtained by applying the initial animation rules setting the alarm time and initializing the event queue with the events mode, mode, select, set, mode. The subsequent animation steps result from applying animation rules for event processing or for moving up and down the state hierarchy.

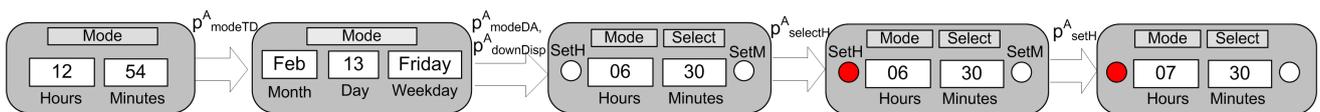


Figure 6: Radio Clock Animation Scenario

4 Semantical Correctness of S2A Transformations

In this section, we continue the general theory of Section 2 and study semantical correctness of $S2A$ -transformations. In our case, semantical correctness of an $S2A$ -transformation means that for each simulation step $G_S \xrightarrow{p_S} H_S$ there is a corresponding animation step $G_A \xrightarrow{p_A} H_A$ where G_A (resp. H_A) are obtained by $S2A$ model transformation from G_S (resp. H_S), and p_A by $S2A$ rule transformation from p_S . Note that this is a special case of semantical correctness defined in [EE05a], where instead of a single step $G_A \xrightarrow{p_A} H_A$ more general sequences $G_A \xrightarrow{*} H_A$ and $H_S \xrightarrow{*} H_A$ are allowed.

the front and the bottom squares are pushouts. Furthermore, we obtain pushouts for the transformation steps $G_i \xrightarrow{q} G_{i+1}$ and $H_i \xrightarrow{q} H_{i+1}$ by composing pushout (PO_I) with the respective pushouts from the double cube. Cases (2) and (3) are handled similarly, with the difference that some morphisms in the respective double cubes are identities. \square

The following notions are used for proving the main Theorem 2.

Definition 7 (Termination of S2AM and Rule Compatibility of S2A) An S2AM transformation $S2AM : VL_S \rightarrow VL_A$ is *terminating* if each transformation $G_S \xrightarrow{Q}^* G_n$ can be extended to $G_S \xrightarrow{Q}^* G_n \xrightarrow{*} G_m$ such that no $q \in Q$ is applicable to G_m anymore. An S2A-transformation $S2A = (S2AM : VL_S \rightarrow VL_A, S2AR : P_S \rightarrow P_A)$ with $S2AM = (VL_S, TG_A, Q)$ is called *rule compatible*, if for all $p_A \in P_A$ and $q \in Q$ we have that p_A and q are parallel and sequential independent.

More precisely, for each $G \xrightarrow{p_A} H$ with $G_S \xrightarrow{Q}^* G$ and $H_S \xrightarrow{Q}^* H$ for some $G_S, H_S \in VL_S$ and each $G \xrightarrow{q} G'$ (resp. $H \xrightarrow{q} H'$) we have parallel (resp. sequential) independence of $G \xrightarrow{p_A} H$ and $G \xrightarrow{q} G'$ (resp. $H \xrightarrow{q} H'$).

Theorem 2 (Semantical Correctness of S2A) *Each S2A transformation $S2A = (S2AM, S2AR)$ is semantically correct, provided that S2A is rule compatible, and S2AM is terminating.*

Proof. Given $S2A = (S2AM : VL_S \rightarrow VL_A, S2AR : P_S \rightarrow P_A)$ with terminating S2AM, a simulation step $G_S \xrightarrow{p_S} H_S$ with $G_S \in VL_S$, and an S2AR transformation sequence $p_S \xrightarrow{Q}^! p_A$ with $p_S = p_0 \xrightarrow{q_0} p_1 \xrightarrow{q_1} \dots \xrightarrow{q_{n-1}} p_n = p_A$ with $n \geq 1$, then we can apply the Local Semantical Correctness Theorem 1 for $i = 0, \dots, n-1$, leading to the diagram below, which includes the case $n = 0$ with $G_S = G_0, H_S = H_0$ and $p_S = p_0 = p_A$, where no $q \in Q$ can be applied to p_S .

$$\begin{array}{ccccccc}
 G_S = G_0 & \xrightarrow{q_0} & G_1 & \xrightarrow{q_1} & G_2 & \xrightarrow{q_2} & \dots \xrightarrow{q_{n-1}} & G_{n-1} & \xrightarrow{q_{n-1}} & G_n \\
 \parallel & & \parallel & & \parallel & & & \parallel & & \parallel \\
 \downarrow p_S = p_0 & \xrightarrow{Q!} & \downarrow p_1 & & \downarrow p_2 & & & \downarrow p_{n-1} & & \downarrow p_n = p_A \\
 H_S = H_0 & \xrightarrow{q_0} & H_1 & \xrightarrow{q_1} & H_2 & \xrightarrow{q_2} & \dots \xrightarrow{q_{n-1}} & H_{n-1} & \xrightarrow{q_{n-1}} & H_n
 \end{array}$$

If no $q \in Q$ can be applied to G_n and H_n anymore, we are ready, because the top sequence is $G_S \xrightarrow{Q}^! G_n = G_A$, and the bottom sequence is $H_S \xrightarrow{Q}^! H_n = H_A$.

Now assume that we have $q_n \in Q$ which is applicable to G_n leading to $G_n \xrightarrow{q_n} G_{n+1}$. Then, rule compatibility implies parallel independence with $G_A \xrightarrow{p_A} H_A$, and the Local Church Rosser Theorem [EEPT06] leads to square (n):

$$\begin{array}{ccccccc}
 G_n & \xrightarrow{q_n} & G_{n+1} & \xrightarrow{\dots} & G_{m-1} & \xrightarrow{q_{m-1}} & G_m = G_A \\
 \parallel p_A & (n) & \parallel p_A & & \parallel p_A & & \parallel p_A \\
 \downarrow & & \downarrow & & \downarrow & & \downarrow \\
 H_n & \xrightarrow{q_n} & H_{n+1} & \xrightarrow{\dots} & H_{m-1} & \xrightarrow{q_{m-1}} & H_m = H_A
 \end{array}$$

This procedure can be repeated as long as rules $q_i \in Q$ are applicable to G_i for $i \geq n$. Since $S2AM$ is terminating, we have some $m > n$ such that no $q \in Q$ is applicable to G_m anymore, leading to a sequence $G_S = G_0 \xrightarrow{Q^!} G_m = G_A$. Now assume that there is some $q \in Q$ which is still applicable to H_m leading to $H_m \xrightarrow{q} H_{m+1}$. Now rule compatibility implies sequential independence of $G_m \xrightarrow{p_A} H_m \xrightarrow{q} H_{m+1}$. In this case, the Local Church Rosser Theorem would lead to a sequence $G_m \xrightarrow{q} G_{m+1} \xrightarrow{p_A} H_{m+1}$ which contradicts the fact that no $q \in Q$ is applicable to G_m anymore. This implies that also $H_0 \xrightarrow{Q^*} H_n \xrightarrow{Q^*} H_m$ is terminating, leading to the required sequence $H_S = H_0 \xrightarrow{Q^!} H_m = H_A$. \square

Extension by Negative Application Conditions

Considering rules with NACs both for the $S2A$ rules in Q (now of the form $q = (N_q \leftarrow L_q \rightarrow R_q)$), and for the simulation rules in P_S (now of the form $p_S = (N_i \leftarrow L \leftarrow I \rightarrow R)$), has the following consequences on the construction of the animation specification by $S2A$ transformation: Def. 3 has to be extended to deal with the additional transformation of NACs in Cases (1) and (2) (in Case (3), the NACs remain unchanged). Moreover, a new Case (4) has to be added covering the case that preconditions (1) - (3) are not satisfied, but there are matches into N_i . Furthermore, the preconditions for all cases now also require the satisfaction of $NAC_q = (L_q \xrightarrow{n} N_q)$. To extend rule compatibility (Def. 7), in addition to parallel and sequential independence in the case without NACs, we have to require that the induced matches satisfy the corresponding NACs. The proof of local semantical correctness of $S2A$ transformations with NACs requires also *NAC-compatibility* of $S2AM$ and $S2AR$ for all $q \in Q$ and $G_i \xrightarrow{p_i} H_i$. *NAC-compatibility* of $S2AM$ means that if q is applicable to a rule p_S , then each match of q in G_i (resp. H_i) satisfies NAC_q . *NAC-compatibility* of $S2AR$ means that if $p_i \xrightarrow{q} p_{i+1}$ satisfies NAC_q , and $G_i \xrightarrow{p_i} H_i$ satisfies $NAC(p_i)$ then $G_{i+1} \xrightarrow{p_{i+1}} H_{i+1}$ satisfies $NAC(p_{i+1})$.

Considering these additional requirements, we can show that each $S2A$ -transformation $S2A = (S2AM, S2AR)$ is semantically correct including NACs, provided that $S2A$ is rule compatible, $S2AM$ is terminating and $S2A$ is *NAC-compatible*. This extends Theorem 2, where now rule compatibility and termination have to be required with NACs (for the complete extended theorem see [EEE06, Erm06]).

Using the extended theorem, we show the semantical correctness of our Radio Clock case study in [EEE06]. Termination is shown to be fulfilled for general $S2A$ transformation systems with suitable rule layers and applied to our case study in [EEE06]. Moreover, it is shown that each $S2AR$ transformation is *NAC-compatible* provided that we have suitable rule layers as in our case study. Thus, it suffices to show only *NAC-compatibility* of $S2AM$ explicitly for the Radio Clock.

5 Related Work

To ensure the correctness of model transformations, Varró et al. [SV03, Var04] use graph transformation rules to specify the dynamic behavior of systems and generate a transition system for each instance model. Based on the transition system, a model checker verifies certain dynamic consistency properties by model checking the source and target models. In [NK06], a method is

presented to verify the semantical equivalence for particular model transformations. It is shown by finding bisimulations that a target model preserves the semantics of the source model with respect to a particular property. This technique does not prove the correctness of the model transformation rules in general, as we propose in this paper for the restricted case of S2A transformation rules. The formal background of bisimulations for graph transformations has been considered also in e.g. [EK04].

For the specification of model transformations, *triple graph grammars* [Sch94] have been frequently used. These grammars are based on a coupling of the syntax rules for the source and target language, which allows derivations in the source language to be translated into derivations of the target language. A third grammar in between source and target produces a mapping structure to keep track of the relation between the source and target structures. Triple graph grammars have been recently used also to model tool integration [KS06] and the integration of multiple views on a system [GDL05]. Here, views are (possibly overlapping) parts of a global alphabet, and graph triples are made of one repository (the complete integrated model), one view and an intermediate graph that relates objects of both. The triple graph grammar specifies the gluing of the views in the repository. This approach has similarities to our approach concerning the relation of simulation and animation alphabets. But the restriction to subtypes of a VL type graph alone is usually not enough to define views which abstract from model details. Given a type graph for Petri nets, for example, it would not be possible to define a view which shows only the markings of particular states and hides the others. In this respect, our approach of S2A transformation is much more flexible. Moreover, our notion of S2AR transformation allows to relate views with behavior.

The animation specification resulting from an S2A transformation provides a good basis for user interaction when defining scenarios in the animation view (e.g. by clicking on a radio clock button to apply an animation rule). Here lies the central advantage of coding the animation view information into the rules instead of translating directly simulation steps into animation steps (as realized e.g. in [HEC03]).

6 Conclusion and Ongoing Work

In this paper we have given a precise definition for simulation-to-animation (S2A) model and rule transformations. The main results show under which conditions an S2A transformation $S2A : SimSpec_{VL_S} \rightarrow AnimSpec_{VL_A}$ is semantically correct in the cases without and with negative application conditions. The results have been used to show semantical correctness of a radio clock case study.

For simplicity, the theory has been presented in the DPO-approach for typed graphs, but it can also be extended to typed attributed graphs, where injective graph morphisms are replaced by suitable classes M and M' of typed attributed graph morphisms for rules and NACs, respectively [EEPT06]. Non DPO-based approaches have not yet been considered.

In addition to analyzing the semantical correctness of S2A, it may be interesting to construct also a backward model and rule transformation $A2S : AnimSpec_{VL_A} \rightarrow SimSpec_{VL_S}$, essentially given by restriction of all graphs and rules to the type graph TG_S . Semantical correctness of A2S means that for each animation step $G_A \xrightarrow{PA} H_A$ there is also a corresponding simulation

step $G_S \xrightarrow{p_S} H_S$ using the restrictions G_S, H_S and p_S of G_A, H_A and p_A , respectively. Finally, we can consider semantical equivalence of $SimSpec_{VL_S}$ and $AnimSpec_{VL_A}$, which requires existence and semantical correctness of $S2A$ and $A2S$, such that both are inverse to each other, i.e. $A2S \circ S2A = Id$ and $S2A \circ A2S = Id$.

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